# Stellar Parameters for Pulsating B-star Candidates in the Kepler Field 

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#### Abstract

The field of asteroseismology has enjoyed a large swath of data coming from recent missions (e.g., CoRoT, Kepler, $K 2$ ). This wealth of new data has allowed the field to expand beyond the previous limitation of a few extremely bright and evolved stars. Asteroseismology relies on accurate surface measurements for boundary conditions, but the predicted physical parameters in the Kepler Input Catalog (KIC) are unreliable for hot stars. We present stellar parameters of 25 candidate pulsating B-star candidates in the Kepler field. We use blue optical spectra to measure the projected rotational velocity ( $V \sin i$ ), effective temperature ( $T_{\text {eff }}$ ), and surface gravity ( $\log g$ ) using TLUSTY and Kurucz ATLAS9 model atmospheres. We find a large discrepancy between our spectroscopically derived parameters and those derived from photometry in the KIC and Gaia Data Release 2 (DR2). Using spectral energy distributions, we also measure the radii of these stars and later calculate the luminosities and masses. We find the extinctions $\left(A_{V}\right)$ of these stars to be consistent with zero, which is expected for stars of high Galactic latitude.


Key words: stars: fundamental parameters - stars: massive - stars: oscillations

## 1. Introduction

Although helioseismology has long proven to be an invaluable tool for calibrating models of the solar interior, general asteroseismological analysis was previously limited to a few extremely bright or evolved stars (Chaplin 2013). With the wide-field, high-precision, Kepler and K2 missions, astronomers are now able to perform asteroseismology on tens of thousands of stars (Chaplin et al. 2011; Yu et al. 2018) across a broad range of temperatures and evolutionary status. Even in its final months, $K 2$ has continued to provide insight into the pulsations of its target stars.

Despite the high Galactic latitude of the original Kepler field, 85 pulsating B-type candidates have been identified in that field (Balona et al. 2011; McNamara et al. 2012). They exhibit a range of nonradial pulsations (NRPs) with periods consistent with $\beta$ Cephei variables, slowly pulsating B stars (SPB), and hybrids between those two classes. The precision light curves available with Kepler are proving to reveal many highfrequency and low-amplitude modes, and with excellent frequency resolution, that are not detectable from the ground.

Asteroseismology of B stars with NRPs is currently being used to improve stellar structure and evolutionary models for hot stars (e.g., Saesen et al. 2010). Their various pulsation frequencies probe different layers of their interiors. Doing so, however requires accurate boundary conditions at the stellar surface (e.g., Huber et al. 2012). Spectroscopy allows accurate measurements of effective temperature, $T_{\text {eff }}$, and surface gravity, $\log g$, that are essential in constraining stellar radii, ages, and evolutionary spin-down rates. Knowledge of the projected rotational velocity, $V \sin i$, is key for studying the angular momentum of NRPs.

One hurdle for the asteroseismic analysis of B-type pulsators in the Kepler field is the lack of accurate physical parameters for these stars. The KIC uses the SDSS $g-r$ color as a temperature indicator, but the Rayleigh-Jeans slope of the hot

[^0]star spectral energy distributions (SEDs) means that the $g-r$ color is largely insensitive to temperature for B-type stars. The KIC photometric $\log g$ measurements are likewise poor since the $g-r$ index does not sample the Balmer jump, which is strongly dependent on atmospheric pressure and thus $\log g$. Balona et al. (2011) used spectroscopic line profile fitting to measure $T_{\text {eff }}$ of 30 B stars in the Kepler field and found substantial differences from the predicted $T_{\text {eff }}$ of the same stars in the KIC (Brown et al. 2011). Pinsonneault et al. (2012) published revised temperature scales for the KIC, but only for stars with $4000 \mathrm{~K} \leqslant T_{\text {eff }} \leqslant 7000 \mathrm{~K}$, which is substantially cooler than the stars considered in this work.
We present here the results of the measurements of $T_{\text {eff }}$, $\log g$, and $V \sin i$ of 25 candidate $\beta$ Cephei, SPB, and hybrid pulsating $B$ stars in the Kepler field with $8 \leqslant V \leqslant 16$. Section 2 details our observations and data reduction of the spectra. In Section 3, we describe our measurements of $T_{\text {eff }}$, $\log g$, and $V \sin i$ of these stars using the Tlusty BSTAR2006 grid and Kurucz ATLAS9 model atmospheres. Comparing $T_{\text {eff }}$ and $\log g$ to the evolutionary tracks of Ekström et al. (2012), we also measure the mass, radius, and age. Section 4 compares our results with the KIC and the Gaia Data Release 2 as well as other published works. Calculated distances from Bailer-Jones et al. (2018) using the Gaia parallaxes are also included in order to estimate extinctions $\left(A_{V}\right)$ for these stars.

## 2. Observations

We observed each target using the KPNO 4 m Mayall telescope with the Ritchey-Chretien (RC) spectrograph from 2014 May 9 to 13 . We used the grating BL 380 in the second order, a $\mathrm{CaSO}_{4}$ order sorting filter, a $1!5$ slit, and the T2KA CCD to achieve resolving power $R=\lambda / \Delta \lambda \approx 7200$. With a central wavelength of $4340 \AA$, this setup allowed us to observe the range $4060-4620 \AA$, covering several useful helium and hydrogen lines. We reduced the raw spectra with the DOSLIT package of Image Reduction and Analysis Facility (IRAF). All spectra were wavelength calibrated using an FeAr arc lamp.

Table 1
Projected Rotational Velocities

| $\begin{aligned} & \text { KIC } \\ & \text { ID } \end{aligned}$ | $\begin{gathered} V \sin i_{4026} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{aligned} & \Delta V \sin \mathrm{i} \\ & \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{aligned}$ | $\begin{gathered} V \sin i_{4388} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{aligned} & \Delta V \sin \mathrm{i} \\ & \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{aligned}$ | $\begin{gathered} V \sin i_{4471} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{aligned} & \Delta V \sin i \\ & \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{aligned}$ | $\begin{gathered} V \sin i_{4481} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{aligned} & \Delta V \sin \mathrm{i} \\ & \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{aligned}$ | $\begin{gathered} V \sin i \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{aligned} & \Delta V \sin i \\ & \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1430353 | 190 | 20 | 195 | 10 | 195 | 12 | 235 | 7 | 210 | 26 |
| 3459297 | .. | $\ldots$ | ... | $\ldots$ | 114 | 10 | 130 | 7 | 123 | 12 |
| 3839930 | 60 | 5 | 50 | 2 | 50 | 2 | 50 | 2 | 51 | 6 |
| 3862353 | 80 | 12 | 55 | 10 | 60 | 5 | 80 | 10 | 64 | 15 |
| 4077252 | ... | ... | ... | ... | 77 | 22 | 62 | 5 | 65 | 23 |
| 4936089 | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | 51 | 6 | 46 | 3 | 48 | 7 |
| 4939281 | 115 | 12 | 100 | 5 | 100 | 15 | 135 | 5 | 115 | 20 |
| 5477601 | . | $\ldots$ | ... | $\ldots$ | 98 | 11 | 86 | 2 | 88 | 11 |
| 7630417 | $\ldots$ | $\ldots$ | 135 | 7 | 130 | 7 | 145 | 12 | 135 | 16 |
| 8167938 | $\ldots$ | $\ldots$ | ... | $\ldots$ | ... | $\cdots$ | 70 | 3 | 70 | 3 |
| 8264293 | ... | $\ldots$ | ... | $\ldots$ | 284 | 5 | 283 | 12 | 284 | 13 |
| 8381949 | 245 | 10 | 245 | 10 | 245 | 15 | ... | $\cdots$ | 245 | 21 |
| 8714886 | 75 | 7 | 45 | 5 | 50 | 2 | 50 | 2 | 52 | 9 |
| 9227988 | ... | $\ldots$ | $\ldots$ | $\cdots$ | 52 | 2 | 48 | 2 | 50 | 3 |
| 9278405 | $\ldots$ | ... | ... | ... | 115 | 16 | 108 | 7 | 110 | 17 |
| 9468611 | ... | $\ldots$ | $\cdots$ | $\ldots$ | 282 | 29 | 258 | 8 | 263 | 30 |
| 9715425 | $\cdots$ | $\ldots$ | 125 | 7 | 125 | 7 | 115 | 7 | 122 | 12 |
| 9910544 | $\ldots$ | $\cdots$ | $\ldots$ | $\cdots$ | 72 | 4 | 72 | 3 | 72 | 5 |
| 9964614 | 85 | 5 | 65 | 5 | 75 | 7 | 85 | 10 | 77 | 14 |
| 10118750 | ... | ... | ... | $\ldots$ | $\ldots$ | $\ldots$ | 271 | 16 | 271 | 16 |
| 10526294 | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | 37 | 9 | 35 | 4 | 36 | 10 |
| 10790075 | ... | $\cdots$ | $\cdots$ | $\cdots$ | 74 | 5 | 70 | 2 | 71 | 5 |
| 11293898 | 355 | 27 | 360 | 17 | 350 | 15 | $\cdots$ | $\cdots$ | 355 | 35 |
| 11360704 | 300 | 7 | 300 | 7 | 300 | 7 | 310 | 7 | 303 | 12 |
| 11671923 | ... | $\ldots$ | $\ldots$ | $\ldots$ | 89 | 6 | 92 | 5 | 91 | 8 |

Table 2
Physical Parameters

| $\begin{aligned} & \text { KIC } \\ & \text { ID } \end{aligned}$ | $T_{\mathrm{eff}}$ $(\mathrm{K})$ | $\begin{gathered} \Delta T_{\mathrm{eff}} \\ (\mathrm{~K}) \end{gathered}$ | $\log g$ <br> (dex) | $\Delta \log g$ (dex) | $\begin{gathered} M_{\star} \\ \left(M_{\odot}\right) \end{gathered}$ | $\begin{gathered} R_{\star} \\ \left(R_{\odot}\right) \end{gathered}$ | $\begin{aligned} & L_{\mathrm{bol}} \\ & \left(L_{\odot}\right) \end{aligned}$ | (Myr) | $\begin{gathered} \mathrm{r} \\ (\mathrm{pc}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1430353 | 17000 | 2000 | 3.30 | 0.27 | $3.888_{-1.73}^{+2.14}$ | $7.31_{-1.30}^{+1.76}$ | 4015-2012 | $42_{-16}^{+30}$ | $7760_{-1293}^{+1782}$ |
| 3459297 | 13100 | 600 | 3.61 | 0.14 | $1.84_{-0.56}^{+1.42}$ | $3.52_{-0.47}^{+1.33}$ | $329{ }_{-99}^{+253}$ | $130_{-22}^{+35}$ | $3463_{-449}^{+599}$ |
| 3839930 | 16950 | 650 | 4.18 | 0.13 | $4.70_{-1.08}^{+1.22}$ | $2.92_{-0.28}^{+0.33}$ | $634_{-142}^{+161}$ | $32_{-19}^{+19}$ | $1763_{-161}^{+195}$ |
| 3862353 | 14000 | 1000 | 3.71 | 0.18 | $2.98{ }_{-1.23}^{+1.66}$ | $3.99_{-0.74}^{+1.05}$ | $551-236$ | $102_{-28}^{+37}$ | $9448{ }_{-1726}^{+2461}$ |
| 4077252 | 12100 | 900 | 3.51 | 0.22 | $1.49_{-0.50}^{+0.52}$ | $3.56{ }_{-0.45}^{+0.48}$ | $244_{-82}^{+86}$ | $179{ }_{-51}^{+53}$ | $2752_{-202}^{+236}$ |
| 4936089 | 12250 | 600 | 4.05 | 0.18 | $1.94{ }_{-0.58}^{+0.42}$ | $2.188_{-0.26}^{+0.13}$ | $96_{-27}^{+18}$ | $103_{-40}^{+59}$ | $1596{ }_{-71}^{+78}$ |
| 4939281 | 17500 | 1000 | 3.87 | 0.14 | $4.77_{-1.17}^{+1.34}$ | $4.20_{-0.42}^{+0.51}$ | $14922_{-393}^{+443}$ | $49_{-12}^{+10}$ | $41033_{-389}^{+476}$ |
| 5477601 | 11950 | 350 | 4.10 | 0.14 | $2.39_{-0.48}^{+0.73}$ | $2.288_{-0.16}^{+0.31}$ | $96_{-16}^{+27}$ | $136{ }_{-39}^{+43}$ | $2134_{-119}^{+133}$ |
| 7630417 | 19200 | 1900 | 3.73 | 0.24 | $4.71_{-2.14}^{+2.73}$ | $4.91_{-0.94}^{+1.29}$ | $2947{ }_{-1428}^{+1799}$ | $33_{-13}^{+18}$ | $10346_{-1883}^{+2640}$ |
| 8167938 | 13400 | 1000 | 4.00 | 0.22 | $9.144_{-3.75}^{+2.64}$ | $5.01_{-0.86}^{+0.46}$ | $728_{-299}^{+211}$ | $111_{-25}^{+51}$ | $1859_{-133}^{+153}$ |
| 8264293 | 13150 | 500 | 4.08 | 0.14 | $2.62_{-0.48}^{+1.61}$ | $2.44_{-0.14}^{+0.73}$ | $161_{-26}^{+98}$ | $105_{-34}^{+34}$ | $1328_{-64}^{+70}$ |
| 8381949 | 20200 | 2000 | 3.72 | 0.27 | $6.744_{-2.84}^{+3.46}$ | $5.944_{-0.96}^{+1.30}$ | $5282_{-2320}^{+2796}$ | $28_{-9}^{+12}$ | $4019{ }_{-603}^{+840}$ |
| 8714886 | 18200 | 900 | 4.10 | 0.14 | $3.47_{-0.67}^{+0.72}$ | $2.755_{-0.18}^{+0.21}$ | $747{ }_{-148}^{+159}$ | $16_{-12}^{+15}$ | $1560_{-95}^{+108}$ |
| 9227988 | 14000 | 1200 | 3.34 | 0.18 | $2.57_{-1.07}^{+1.37}$ | $5.688_{-1.06}^{+1.42}$ | $1114_{-505}^{+627}$ | $93_{-31}^{+50}$ | $6799_{-1174}^{+1642}$ |
| 9278405 | 11100 | 200 | 4.14 | 0.11 | $2.11_{-0.31}^{+0.31}$ | $2.05{ }_{-0.10}^{+0.10}$ | $57_{-6}^{+6}$ | $173_{-35}^{+35}$ | $654_{-18}^{+19}$ |
| 9468611 | 11200 | 600 | 3.90 | 0.22 | $1.85{ }_{-0.55}^{+0.80}$ | $2.533_{-0.25}^{+0.47}$ | $90_{-23}^{+37}$ | $224_{-76}^{+66}$ | $2729{ }_{-254}^{+310}$ |
| 9715425 | 15750 | 750 | 3.52 | 0.27 | $2.144_{-0.97}^{+1.24}$ | $4.21_{-0.77}^{+1.08}$ | $982_{-386}^{+523}$ | $67_{-22}^{+30}$ | $6059{ }_{-1101}^{+1547}$ |
| 9910544 | 12100 | 300 | 4.10 | 0.14 | $4.21_{-0.76}^{+0.80}$ | $3.03_{-0.17}^{+0.19}$ | $177_{-24}^{+26}$ | $184_{-18}^{+16}$ | $1294{ }_{-70}^{+79}$ |
| 9964614 | 20100 | 850 | 3.84 | 0.14 | $6.62_{-1.95}^{+2.39}$ | $5.13_{-0.66}^{+0.85}$ | $3862_{-1109}^{+1371}$ | $29_{-5}^{+3}$ | $3407{ }_{-427}^{+561}$ |
| 10118750 | 10950 | 500 | 4.27 | 0.22 | $2.944_{-0.89}^{+0.99}$ | $2.08_{-0.21}^{+0.26}$ | $56_{-14}^{+16}$ | $196_{-110}^{+98}$ | $3319{ }_{-329}^{+405}$ |
| 10526294 | 11500 | 500 | 4.18 | 0.14 | $3.266_{-0.73}^{+0.81}$ | $2.43_{-0.21}^{+0.25}$ | $93_{-20}^{+23}$ | $189{ }_{-66}^{+58}$ | $3025_{-251}^{+297}$ |
| 10790075 | 11850 | 400 | 3.63 | 0.14 | $2.288_{-0.77}^{+0.92}$ | $3.833_{-0.59}^{+0.72}$ | $260_{-84}^{+101}$ | $184{ }_{-43}^{+34}$ | $4153_{-536}^{+699}$ |
| 11293898 | 16400 | 1000 | 3.79 | 0.18 | $0.92_{-0.25}^{+0.28}$ | $2.02_{-0.21}^{+0.25}$ | $266_{-74}^{+82}$ | $58_{-10}^{+18}$ | $3823_{-374}^{+459}$ |
| 11360704 | 16500 | 1050 | 3.72 | 0.14 | $7.26_{-2.08}^{+2.55}$ | $6.16_{-0.77}^{+0.99}$ | 2532 ${ }_{-797}^{+947}$ | $52_{-12}^{+22}$ | $3428_{-414}^{+537}$ |
| 11671923 | 11800 | 200 | 4.05 | 0.11 | $2.96_{-0.50}^{+0.50}$ | $2.69_{-0.17}^{+0.17}$ | $127{ }_{-17}^{+17}$ | $188_{-19}^{+17}$ | $1065_{-49}^{+53}$ |

Table 3
Comparison of Stellar Parameters of Kepler B Stars

| KIC <br> ID | KIC |  | DR2 <br> $T_{\text {eff }}$ <br> (K) | Other |  | This Work |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & T_{\text {eff }} \\ & (\mathrm{K}) \end{aligned}$ | $\log g$ <br> (dex) |  | $\begin{aligned} & T_{\text {eff }} \\ & (\mathrm{K}) \end{aligned}$ | $\log g$ <br> (dex) | $\begin{aligned} & T_{\text {eff }} \\ & (\mathrm{K}) \end{aligned}$ | $\log g$ <br> (dex) |
| 1430353 | 10765 | 3.653 | $95855_{-73}^{+106}$ | $\ldots$ | $\cdots$ | $17000 \pm 2000$ | $3.30 \pm 0.27$ |
| 3459297 | 10592 | 4.629 | $9365_{-3148}^{+248}$ | $13430 \pm 250^{\text {a }}$ | $3.8 \pm 0.1^{\text {a }}$ | $13100 \pm 600$ | $3.61 \pm 0.14$ |
| 3839930 | 11272 | 4.277 | $8712_{-1039}^{+774}$ | $16500 \pm 1000^{\text {b }}$ | $4.2 \pm 0.3^{\text {b }}$ | $16950 \pm 650$ | $4.18 \pm 0.13$ |
| 3862353 | 10738 | 4.025 | $9623_{-733}^{+194}$ | $\ldots$ | $\ldots$ | $14000 \pm 1000$ | $3.71 \pm 0.18$ |
| 4077252 | 10514 | 3.948 | $9312_{-283}^{+282}$ | $\ldots$ | $\ldots$ | $12100 \pm 900$ | $3.51 \pm 0.22$ |
| 4936089 | 11295 | 4.275 | $9554_{-2140}^{+101}$ | $\ldots$ | $\ldots$ | $12250 \pm 600$ | $4.05 \pm 0.18$ |
| 4939281 | 11298 | 4.316 | $8726_{-3928}^{+943}$ | $\ldots$ | $\ldots$ | $17500 \pm 1000$ | $3.87 \pm 0.14$ |
| 5477601 | 10906 | 4.138 | $9304{ }_{-227}^{+275}$ | $\ldots$ | $\ldots$ | $11950 \pm 350$ | $4.10 \pm 0.14$ |
| 7630417 | 10449 | 4.581 | $9613_{-90}^{+128}$ | $\cdots$ | $\ldots$ | $19200 \pm 1900$ | $3.73 \pm 0.24$ |
| 8167938 | 11167 | 4.228 | $9453-31545$ | $12300 \pm 800^{\text {b }}$ | $4.0 \pm 0.3^{\text {b }}$ | $13400 \pm 1000$ | $4.00 \pm 0.22$ |
| 8264293 | 10038 | 4.458 | $9530_{-2116}^{+170}$ | $\cdots$ | $\cdots$ | $13150 \pm 500$ | $4.08 \pm 0.14$ |
| 8381949 | 9782 | 4.394 | $9020_{-4222}^{+680}$ | $24500 \pm 1400^{\text {b }}$ | $4.3 \pm 0.3^{\text {b }}$ | $20200 \pm 2000$ | $3.72 \pm 0.27$ |
| 8714886 | 9142 | 4.093 | $9351_{-209}^{+260}$ | $19000 \pm 1200^{\text {b }}$ | $4.3 \pm 0.3^{\text {b }}$ | $18200 \pm 900$ | $4.10 \pm 0.14$ |
| 9227988 | 10890 | 4.023 | $9546{ }_{-2301}^{+60}$ | ... | $\ldots$ | $14000 \pm 1200$ | $3.34 \pm 0.18$ |
| 9278405 | 11486 | 4.199 | $8614_{-1687}^{+1048}$ | $\ldots$ | $\ldots$ | $11100 \pm 200$ | $4.14 \pm 0.11$ |
| 9468611 | 11063 | 3.735 | $9365_{-3148}^{+248}$ | $\cdots$ | $\ldots$ | $10750 \pm 550$ | $3.70 \pm 0.22$ |
| 9715425 | 11199 | 4.114 | $8728_{-3930}^{+964}$ | $\ldots$ | $\ldots$ | $15750 \pm 1500$ | $3.52 \pm 0.27$ |
| 9910544 | 10698 | 4.079 | $9540_{-629}^{+202}$ | . ${ }^{\text {a }}$ | . $\cdot$ | $12100 \pm 300$ | $4.10 \pm 0.14$ |
| 9964614 | 8915 | 4.067 | $88699_{-906}^{+724}$ | $20300 \pm 1200^{\text {b }}$ | $3.9 \pm 0.2^{\text {b }}$ | $20100 \pm 850$ | $3.84 \pm 0.14$ |
| 10118750 | 11147 | 3.751 | $9045_{-2663}^{+521}$ | ... | ... | $10950 \pm 500$ | $4.27 \pm 0.22$ |
| 10526294 | 11072 | 3.743 | $8983{ }_{-1563}^{+743}$ | $\ldots$ | $\ldots$ | $11500 \pm 500$ | $4.18 \pm 0.14$ |
| 10790075 | 11396 | 3.771 | $9055_{-2005}^{+637}$ | $\ldots$ | $\ldots$ | $11850 \pm 400$ | $3.63 \pm 0.14$ |
| 11293898 | 15072 | 4.932 | $8599_{-1179}^{+994}$ | ... | ... | $16400 \pm 1000$ | $3.79 \pm 0.18$ |
| 11360704 | 12400 | 4.934 | $8869{ }_{-906}^{+724}$ | $20700 \pm 1200^{\text {b }}$ | $4.1 \pm 0.3^{\text {b }}$ | $16500 \pm 1050$ | $3.72 \pm 0.14$ |
| 11671923 | 10044 | 4.237 | $9285{ }_{-1643}^{+441}$ | ... | ... | $11800 \pm 200$ | $4.05 \pm 0.11$ |

## Notes.

${ }^{\text {a }}$ Pápics et al. (2017).
${ }^{\mathrm{b}}$ Balona et al. (2011).

## 3. Spectral Modeling

Two grids of synthetic spectra were used in our modeling process to measure $T_{\text {eff }}, \log g$, and $V \sin i$. First, we used a grid of line blanketed, plane-parallel, local thermodynamic equilibrium (LTE) models generated using the ATLAS9 code (Kurucz 1994) for stars with $T_{\text {eff }}<15,000 \mathrm{~K}$. The non-LTE (NLTE) Tlusty BSTAR2006 (Lanz \& Hubeny 2007) model spectra were used for stars with $T_{\text {eff }}>15,000 \mathrm{~K}$. We adopted grids of $\left(Z / Z_{\odot}=1\right)$ and a microturbulent velocity of $V_{t}=2 \mathrm{~km} \mathrm{~s}^{-1}$.

Before fitting, we estimated $T_{\text {eff }}$ and $\log g$ of the stars based on the strength and shapes of the Balmer and helium lines. We measured the projected rotational velocity ( $V \sin i$ ) using custom interactive data language (IDL) codes to compare the observed profiles of He II $\lambda 4026$, He I $\lambda \lambda 4387,4471$, and Mg II $\lambda 4481$ to limb-darkened, rotationally broadened, and instrumentally broadened model profiles using steps of $10 \mathrm{~km} \mathrm{~s}^{-1}$. For each step, we compared $\Sigma(O-C)^{2}$, the sum of the squares of the residuals, and determined the minimal value of a parabolic fit as the value for $V \sin i$. The error in $V \sin i$ was determined by allowing a $5 \%$ tolerance in $\Sigma(O-C)^{2}$. Table 1 lists the measurements of $V \sin i$ for all of the helium lines as well as their weighted averages.

We then modeled $\mathrm{H} \gamma$ lines for $T_{\text {eff }}$ and $\log g$ using broadened models according to our measured $V \sin i$ along each point in our generated ATLAS9 grid or BSTAR2006 gird. Once we found the closest match with the grid, we used linear
interpolation between the grid points to find the best fit for $T_{\text {eff }}$ and $\log g$. The errors in $T_{\text {eff }}$ and $\log g$ were determined by allowing a $5 \%$ tolerance of the $\Sigma(O-C)^{2}$. Our $T_{\text {eff }}$ and $\log g$ measurements are recorded in Table 2.

## 4. Discussion

As expected, we find large discrepancies between photometrically derived $T_{\text {eff }}$ and $\log g$ and our measurements. In columns 2 and 3 of Table 3, we show the derived $T_{\text {eff }}$ and $\log g$ from the KIC for our observed stars (Brown et al. 2011). We include in column 4 of Table 3 the $T_{\text {eff }}$ from the recently released DR2 (Andrae et al. 2018). Columns 7 and 8 of this table give our measurements using spectroscopic fitting as well as the uncertainties for these values.

We also include in columns 5 and 6 of Table 3 some revised measurements from Balona et al. (2011) and Pápics et al. (2017). Balona et al. (2011) used metal-line blanketed LTE models to model their stars following the methods described by $\emptyset$ stensen et al. (2010). The biggest reason for the discrepancy with our results and those from Balona et al. (2011) is that they assume $V \sin i \sim 0 \mathrm{~km} \mathrm{~s}^{-1}$ for all of their measurements. As a result, they overestimate $T_{\text {eff }}$ and $\log g$ significantly for stars with large $V \sin i$, which leads to wider, shallower hydrogen lines which peak in strength around $10,000 \mathrm{~K}$. Pápics et al. (2017) used the BSTAR2006 synthetic spectra


Figure 1. Comparison of our results with Balona et al. (2011) and Pápics et al. (2017) for temperature (a) and surface gravity (b). The horizontal and vertical error bars in these figures are the calculated errors from this work, Balona et al. (2011), and Pápics et al. (2017), respectively. The symbol size is proportional to our measured $V \sin i$ to highlight the discrepancies between our results and those of other works.


Figure 2. Hertzsprung-Russel (HR) diagram of observed stars using the evolutionary tracks from Ekström et al. (2012). The values associated with each track are in solar masses. All stars to the left of the black dotted line ( $T_{\text {eff }}>15,000 \mathrm{~K}$ ) were modeled using the BSTAR2006 grid of model spectra. Those on the right ( $T_{\text {eff }}<15,000 \mathrm{~K}$ ) were modeled using the ATLAS9 models.
(Lanz \& Hubeny 2007) to measure the fundamental parameters of KIC 3459297. They also find $V \sin i=109 \pm 14 \mathrm{~km} \mathrm{~s}^{-1}$ for KIC 3459297, which agrees with our measurements. Figure 1 compares our results for $T_{\text {eff }}$ and $\log g$ with those from Balona et al. (2011) and Pápics et al. (2017). To emphasize the dependency on $V \sin i$, the sizes of the symbols are proportional to our measured value of $V \sin i$.

Using our measured $T_{\text {eff }}$ and $\log g$, we can compare model SEDs to photometric data to calculate the radii of our stars using

$$
\begin{equation*}
F_{\nu} / \mathfrak{F}_{\nu}=\left(R_{\star} / r\right)^{2}, \tag{1}
\end{equation*}
$$

where $F_{\nu}$ is the apparent monochromatic flux, $\mathfrak{F}_{\nu}$ is the absolute flux at the surface of the star, and $r$ is the distance to the star. $F_{\nu}$ was calculated by converting the $J, H$, and $K$ band magnitudes
from the Two Micron All-Sky Survey (2MASS; Skrutskie et al. 2006) to fluxes using the zero-points from Cohen et al. (2003). $\mathfrak{F}_{\nu}$ was determined using model SEDs with our measured $T_{\text {eff }}$ and $\log g$. We assumed no interstellar extinction $\left(A_{V}\right)$ during this process, as these stars are above the Galactic plane where we would expect low $A_{V}$ values and they would have negligible effects in the $J, H$, and $K$ bands. We used the BSTAR2006 models (Lanz \& Hubeny 2007) for stars with $T_{\text {eff }}>15,000 \mathrm{~K}$ and ATLAS models (Castelli \& Kurucz 2004) for stars with $T_{\text {eff }}<15,000 \mathrm{~K}$. The distances were calculated by Bailer-Jones et al. (2018) by converting the parallaxes measured in DR2 using Bayesian statistics. Our error bars were calculated by propagating the errors from $r, T_{\text {eff }}$, and $\log g$. We then used our measured $\log g$ and $R_{\star}$ to calculate the masses $\left(M_{\star}\right)$ of our stars. KIC 11293898 likely has an underestimated mass, for reasons we discuss later in this work.

Using the non-rotating evolutionary tracks of Ekström et al. (2012), we calculated an approximate age of the stars by interpolating between tracks using $T_{\text {eff }}$ and $R_{\star}$. In Table 2, we include our measured $R_{\star}, M_{\star}$ and age $\left(\tau_{\star}\right)$, as well as the calculated bolometric luminosity ( $L_{\mathrm{bol}}$ ) and the distances from Bailer-Jones et al. (2018). We compare our $T_{\text {eff }}$ and $\log g$ to the non-rotating evolutionary tracks of Ekström et al. (2012) in Figure 2. Our measured $M_{\star}$ and $R_{\star}$ are consistent with their positions along these evolutionary tracks for most stars.

The apparent magnitudes ( $V$ ), bolometric absolute magnitudes ( $M_{\text {bol }}$ ), bolometric corrections (BC), absolute magnitudes $\left(M_{V}\right)$, and calculated $A_{V}$ are all listed in Table 4. The $V$ values in column 6 are from the SIMBAD database with an assumed uncertainty of 0.1 mag , and the BC values in column 3 are interpolated from Flower (1996) and Torres (2010). Using $r, V$, and our measurements, we can estimate $A_{V}$. The extinctions are calculated using

$$
\begin{equation*}
A_{V}=V-M_{V}+5-5 \log r \tag{2}
\end{equation*}
$$

We find that $A_{V}$ is consistent with the 3D dust map provided by Green et al. (2018).

Table 4
Photometry

| $\begin{aligned} & \text { KIC } \\ & \text { ID } \end{aligned}$ | $\begin{gathered} M_{\mathrm{bol}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \mathrm{BC} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{aligned} & \Delta \mathrm{BC} \\ & (\mathrm{mag}) \end{aligned}$ | $\begin{gathered} M_{V} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} V \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A_{V} \\ (\mathrm{mag}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1430353 | $-4.28_{-1.21}^{+1.45}$ | -1.53 | 0.61 | $-2.75{ }_{-1.36}^{+1.57}$ | 12.71 | $1.01_{-1.6}^{+1.95}$ |
| 3459297 | $-1.56_{-0.73}^{+0.93}$ | -0.90 | 0.27 | $-0.66_{-0.78}^{+0.97}$ | $\ldots$ | ... |
| 3839930 | $-2.27_{-0.54}^{+0.62}$ | -1.52 | 0.20 | $-0.75_{-0.58}^{+0.65}$ | 10.79 | $0.31_{-0.73}^{+0.86}$ |
| 3862353 | $-2.12_{-1.06}^{+1.41}$ | -1.07 | 0.41 | $-1.05_{-1.14}^{+1.47}$ | ... | ... |
| 4077252 | $-1.24_{-0.67}^{+0.7}$ | -0.70 | 0.43 | $-0.54_{-0.8}^{+0.83}$ | 12.29 | $0.63_{-0.88}^{+0.93}$ |
| 4936089 | $-0.23_{-0.43}^{+0.44}$ | -0.73 | 0.29 | $0.51_{-0.52}^{+0.53}$ | 11.93 | $0.41_{-0.56}^{+0.58}$ |
| 4939281 | $-3.2{ }_{-0.64}^{+0.72}$ | -1.60 | 0.30 | $-1.611_{-0.7}^{+0.78}$ | ... | ... |
| 5477601 | $-0.22_{-0.35}^{+0.38}$ | -0.67 | 0.17 | $0.455_{-0.39}^{+0.42}$ | $\ldots$ | $\ldots$ |
| 7630417 | $-3.94{ }_{-1.17}^{+1.48}$ | -1.80 | 0.50 | $-2.14{ }_{-1.28}^{+1.56}$ | $\ldots$ | $\cdots$ |
| 8167938 | $-2.43_{-0.66}^{+0.69}$ | -0.96 | 0.43 | $-1.46_{-0.79}^{+0.82}$ | 10.77 | $0.89_{-0.87}^{+0.92}$ |
| 8264293 | $-0.79_{-0.37}^{+0.39}$ | -0.91 | 0.22 | $0.13_{-0.43}^{+0.45}$ | 11.26 | $0.52_{-0.5}^{+0.52}$ |
| 8381949 | $-4.58_{-1.06}^{+1.28}$ | -1.91 | 0.50 | $-2.66_{-1.17}^{+1.38}$ | 10.96 | $0.6{ }_{-1.39}^{+1.73}$ |
| 8714886 | $-2.45_{-0.48}^{+0.51}$ | -1.68 | 0.25 | $-0.77_{-0.54}^{+0.57}$ | 10.86 | $0.66_{-0.62}^{+0.66}$ |
| 9227988 | $-2.89_{-1.08}^{+1.37}$ | -1.07 | 0.49 | $-1.82_{-1.18}^{+1.45}$ | 12.54 | $0.19_{-1.46}^{+1.89}$ |
| 9278405 | $0.33_{-0.19}^{+0.2}$ | -0.49 | 0.10 | $0.82{ }_{-0.22}^{+0.22}$ | 10.16 | $0.26_{-0.26}^{+0.27}$ |
| 9468611 | $-0.16_{-0.61}^{+0.7}$ | -0.51 | 0.30 | $0.35_{-0.69}^{+0.76}$ | ... | ... |
| 9715425 | $-2.75{ }_{-1.16}^{+1.46}$ | -1.35 | 0.51 | $-1.4{ }_{-1.26}^{+1.55}$ | $\ldots$ | ... |
| 9910544 | $-0.89_{-0.33}^{+0.36}$ | -0.70 | 0.14 | $-0.19_{-0.36}^{+0.39}$ | 10.80 | $0.43{ }_{-0.45}^{+0.49}$ |
| 9964614 | $-4.24_{-0.7}^{+0.88}$ | -1.90 | 0.22 | $-2.33_{-0.73}^{+0.91}$ | 10.61 | $0.28{ }_{-0.97}^{+1.23}$ |
| 10118750 | $0.36{ }_{-0.6}^{+0.7}$ | -0.46 | 0.25 | $0.811_{-0.65}^{+0.74}$ | ... | ... |
| 10526294 | $-0.19_{-0.53}^{+0.59}$ | $-0.58$ | 0.25 | $0.38_{-0.58}^{+0.64}$ | $\cdots$ | . ${ }^{\text {a }}$ |
| 10790075 | $-1.31_{-0.69}^{+0.88}$ | -0.65 | 0.20 | $-0.66_{-0.72}^{+0.9}$ | 12.96 | $0.53_{-0.97}^{+1.23}$ |
| 11293898 | $-1.33_{-0.67}^{+0.76}$ | -1.45 | 0.32 | $0.12_{-0.74}^{+0.82}$ | ... | ... |
| 11360704 | $-3.78_{-0.77}^{+0.92}$ | -1.46 | 0.34 | $-2.32_{-0.84}^{+0.98}$ | 10.62 | $0.26{ }_{-1.03}^{+1.25}$ |
| 11671923 | $-0.53_{-0.26}^{+0.28}$ | -0.64 | 0.10 | $0.11_{-0.28}^{+0.3}$ | 10.58 | $0.33_{-0.36}^{+0.39}$ |

As mentioned before, we noticed our calculated mass for KIC 11293898 to be extremely low compared to its measured effective temperature. Using the non-rotated evolutionary tracks from Ekström et al. (2012), we can measure $M_{\star}$ and $R_{\star}$ based on $T_{\text {eff }}$ and $\log g$. We find $R_{\star}=5.16 R_{\odot}$ and $M_{\star}=5.98 M_{\odot}$ for KIC 11293898. Using this $R_{\star}$, we find $r=9752 \mathrm{pc}$, which is well over twice the value calculated by Bailer-Jones et al. (2018).

Our goal with this publication is to improve the measurements of fundamental parameters for pulsating B-type stars in the Kepler survey. Using model fitting with the Tlusty BSTAR2006 grid and Kurucz ATLAS9 model atmospheres, as well as the use of evolutionary tracks from Ekström et al. (2012), we measured $T_{\text {eff }}, \log g, V \sin i, M_{\star}, \tau_{\star}, R_{\star}$, and $L_{\mathrm{bol}}$ for 25 pulsating B-type stars. We find that the $T_{\text {eff }}$ and $\log g$ measurements from KIC and DR2 are unreliable for these hot stars and that improved stellar parameters are required to continue asteroseismic analysis of these stars.
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This research has made use of the SIMBAD database, operated at CDS, Strasbourg, France.

Facilities: Mayall (RC spectrograph).
Software: IRAF, IDL.

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